MCSM Assignment 9 Problem 7.45 Saurabh Kumar

Gibbs sampler is based on conditional distributions derived from  $f(x_1,...,x_q)$  or  $g(y_1,...,y_p)$ .

These conditional distributions may be well defined and may be simulated from, but may not correspond to any joint distribution g; that is the function g is not integrable. The same problem may occur when using a proportionality relation; that is,  $\pi(\theta|x)$  is proportional to  $\pi(\theta)f(x|\theta)$ , to derive a Metropolis-Hastings algorithm for  $\pi(\theta)f(x|\theta)$ .

In the given problem, function g is not integrable. So Metropolis-Hastings algorithm cannot be used and hence Gibbs sampler cannot be implemented.